

Hadron and Nuclear Physics

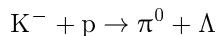
Exercise sheet 5

Winter term 2013/14

Hand-in: Monday, Jan 13th 2014, **13:00**, Room 108

Problem 5.1: Energy- without Momentum-Transfer (9 points)

The following elementary-particle reaction may be carried out on a proton target at rest in the laboratory:



Find the special value of the incident K^- energy such that the Λ can be produced at rest in the laboratory. Your answer should be expressed in terms of rest masses m_{π^0} , m_{K^-} , m_p , m_Λ .

Problem 5.2: Deuteron (9 points)

The deuteron is a bound state of a proton and a neutron of total angular momentum $J = 1$. It is known to be principally an S ($l = 0$) state with a small admixture of a D ($l = 2$) state.

- (a) Explain why a P state cannot contribute.
- (b) Explain why a G state cannot contribute.

Problem 5.3: Pion capture (9 points)

A π^- ($J^P = 0^-$) is initially bound in the lowest-energy Coulomb wave function around a deuteron. It is captured by the deuteron (a proton and a neutron in 3S_1 state), which is converted into a pair of neutrons:



- (a) What is the orbital angular momentum of the neutron pair?
- (b) What is the total spin S ?
- (c) What is the probability for finding both neutron spins directed opposite to the spin of the deuteron?

Problem 5.4: Dalitz-Plots (9 points)

CLEO-c was an experiment at the Cornell Electron Storage Ring (CESR) which examined open-charm mesons produced in the reactions $e^+e^- \rightarrow \psi(3770) \rightarrow D^0\bar{D}^0$ and $e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$. What resonances are visible in the CLEO Dalitz-plot (and the corresponding mass projections) of the decay $D^0 \rightarrow K^-\pi^+\pi^0$? Also calculate the minimum and maximum allowed value of $M^2(K^-\pi^+)$ and $M^2(\pi^+\pi^0)$.

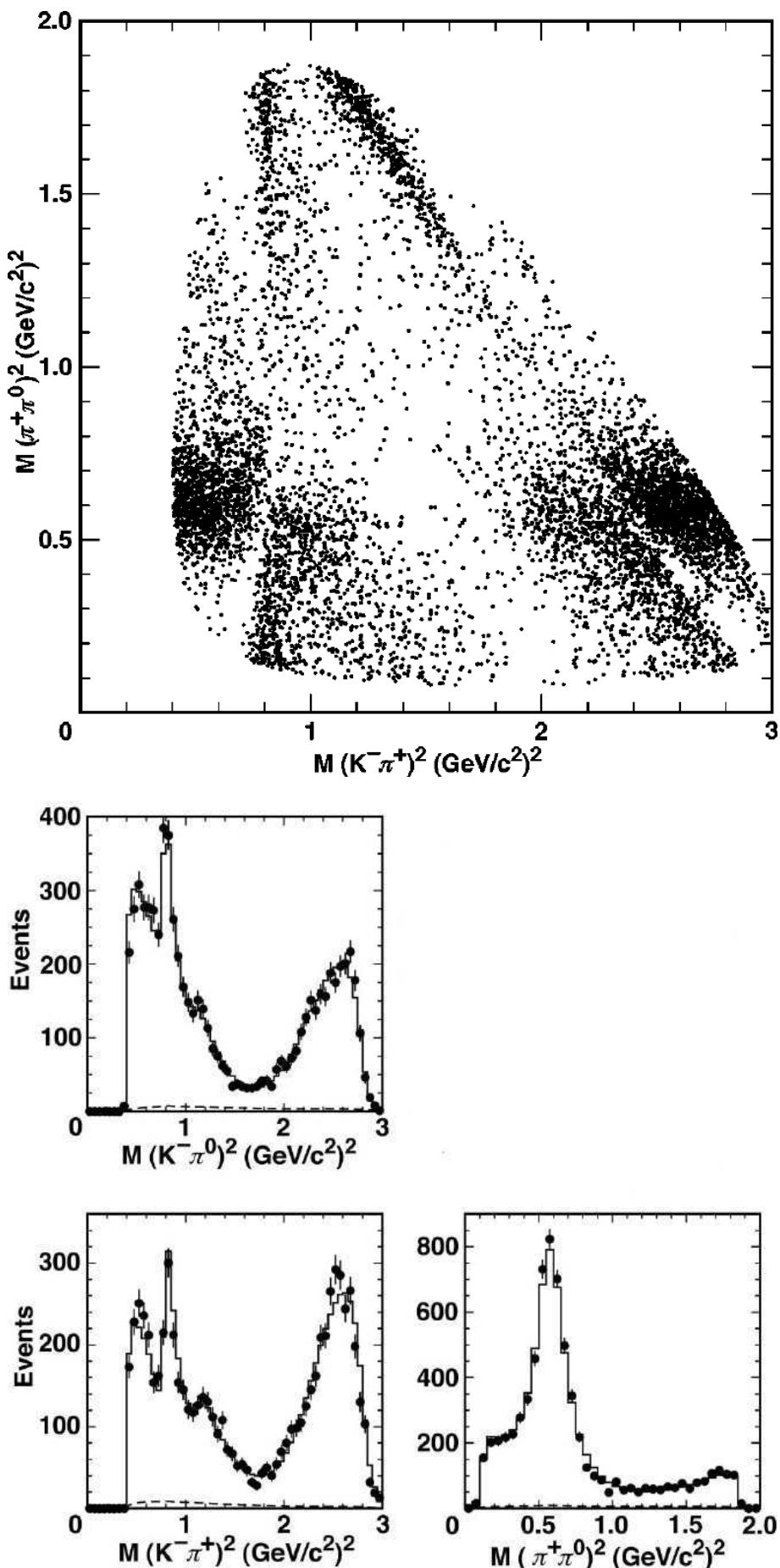
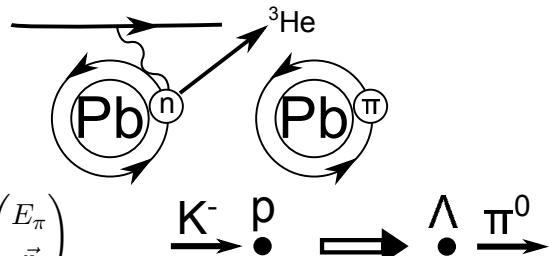


Figure 1: Dalitz-plot for the decay $D^0 \rightarrow K^-\pi^+\pi^0$ and the mass projections.

5 Übung: Besprechung

5.1 Aufgabe

$$\begin{aligned}
 K^- + p &\rightarrow \pi^0 + \Lambda \\
 \text{4-Impuls: } \begin{pmatrix} E_k \\ \vec{p} \end{pmatrix} + \begin{pmatrix} m_p \\ \vec{0} \end{pmatrix} &= \begin{pmatrix} m_\Lambda \\ \vec{0} \end{pmatrix} + \begin{pmatrix} E_\pi \\ \vec{p} \end{pmatrix} \\
 \Rightarrow p_K + p_p &= p_\Lambda + p_\pi \Leftrightarrow p_K^2 + p_p^2 + 2p_p p_K = p_\Lambda^2 + p_\pi^2 + 2p_\Lambda p_\pi \\
 \Leftrightarrow m_K^2 + m_p^2 + 2E_K m_p &= m_\Lambda^2 + m_\pi^2 + 2E_\pi m_\Lambda \\
 E_\pi &= E_K + m_p - m_\Lambda \\
 \Rightarrow 2E_K m_p &= m_\pi^2 + m_\Lambda^2 - m_K^2 - m_p^2 + 2E_K m_\Lambda + 2m_\Lambda m_p - 2m_\Lambda^2 \\
 \Leftrightarrow 2E_K(m_p - m_\Lambda) &= m_\pi^2 - m_K^2 - m_\Lambda^2 - m_p^2 + 2m_\Lambda m_p \\
 \Leftrightarrow E_K &= \frac{m_K^2 - m_\pi^2 + (m_\Lambda - m_p)^2}{2(m_\Lambda - m_p)} = 724,21 \text{ MeV}
 \end{aligned}$$



5.2 Aufgabe

siehe Abgabe

5.3 Aufgabe

ab) $\pi^- + d \rightarrow n + n$

$$0^- + 1^+ \rightarrow 0^+ + 0^+$$

$$\eta_\pi \cdot \eta_d \cdot (-1)^L = \eta_n^2 \cdot (-1)^{L'}$$

Mit η intrinsische Parität und L Bahndrehimpuls.

Das Pion ist im niedrigsten Energiezustand $\Rightarrow L = 0$

$$\Rightarrow -1 = (-1)^{L'} \Rightarrow L' = 1, 3, 5, \dots$$

2 identische Fermionen \Rightarrow Streuwellenfunktion Ψ asymmetrisch.

$$\Psi = \Psi_{\text{ort}} \cdot \Psi_{\text{spin}}$$

Negative Parität $\Rightarrow \Psi_{\text{ort}}$ asymmetrisch (-)

$\Rightarrow \Psi_{\text{spin}}$ symmetrisch (+).

$S = 0 \Rightarrow$ Singulett asymmetrisch

$S = 1 \Rightarrow$ Triplet symmetrisch

$$\Rightarrow S = 1.$$

$$|L' - 1| \leq J \leq |L' + 1|$$

$$\Rightarrow L' = 1$$

c) 1. Möglichkeit: Betrachte z-Komponente des Spins:

$$J_z = 1(\text{oben}) = L_z + S_z = L_z - 1(\text{unten})$$

$$\Rightarrow L_z = 2 \notin \{-1, 0, 1\} \text{ (a)} \not\vdash$$

2. Möglichkeit: Clebsch Gordan Spin Funktionen:

$$|S_n, S_{n,z}\rangle |S_n, S_{n,z}\rangle = |\frac{1}{2}, -\frac{1}{2}\rangle |\frac{1}{2}, -\frac{1}{2}\rangle = |1, -1\rangle = |S, S_z\rangle$$

$$|\phi\rangle = |S, S_z\rangle |L, L_z\rangle = |1, -1\rangle |1, 1\rangle = \frac{1}{\sqrt{6}} |2, 0\rangle - \frac{1}{\sqrt{2}} |1, 0\rangle + \frac{1}{\sqrt{3}} |0, 0\rangle$$

Aufenthaltswahrscheinlichkeit des Spinzustandes in der Reaktion:

$$\langle 1, 1 | \phi \rangle = 0$$

5.4 Aufgabe

Siehe Abgabe.

Hinweis zur Vorgehensweise: Hier zunächst $\pi^+\pi^0$ Plot. Hier ist Peak am eindeutigsten und es lässt sich $D^0 \rightarrow \rho^+ K^- \rightarrow K^-\pi^+ + \pi^0$ sehen.